

# Warm-Up

1. For the translation  $(x, y) \rightarrow (x - 5, y + 4)$ , tell where the image for quadrilateral pre-image ABCD would be located.

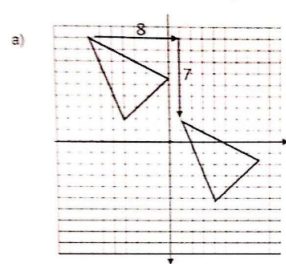
A  $(-4, 6) \rightarrow A'$  \_\_\_\_\_ C  $(-3, 1) \rightarrow C'$  \_\_\_\_\_

B  $(-8, 7) \rightarrow B'$  \_\_\_\_\_ D  $(-2, 2) \rightarrow D'$  \_\_\_\_\_

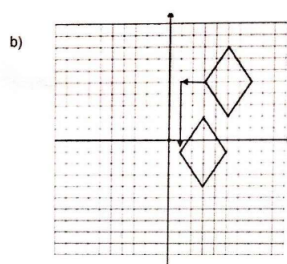
Advanced Geometry  
Section 1.1 Translations Homework

Name \_\_\_\_\_

1. Describe each of the translations below. Then, write the transformation rule that maps the pre-image onto the image.



$$(x, y) \rightarrow (x + 5, y - 7)$$



$$(x, y) \rightarrow (x + 5, y + 1)$$

2. a) Name the coordinates of the pre-image to the right.

A  $(-4, 1)$  B  $(-1, 1)$   
C  $(-3, -2)$  D  $(-4, -2)$

- b) Use arrow notation to write a rule for the given translation.

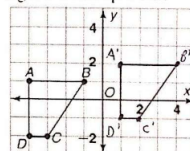
$$(x, y) \rightarrow (x + 5, y + 1)$$

- c) Graph and label the image after the translation.

- d) Name the coordinates of the image.

A'  $(1, 2)$  B'  $(4, 2)$   
C'  $(2, -1)$  D'  $(1, -1)$

right 5 units, up 1 unit

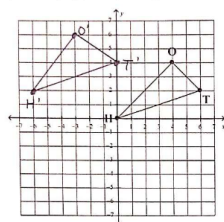


3. MULTIPLE CHOICE: Write a description of the rule  $(x, y) \rightarrow (x - 7, y + 4)$ .

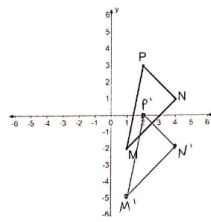
- (a) translation 7 units to the right and 4 units up  
(b) translation 7 units to the left and 4 units down  
(c) translation 7 units to the right and 4 units down  
(d) translation 7 units to the left and 4 units up

4. Apply the given transformation to each triangle below. Label the images appropriately.

a)  $(x, y) \rightarrow (x - 6, y + 2)$

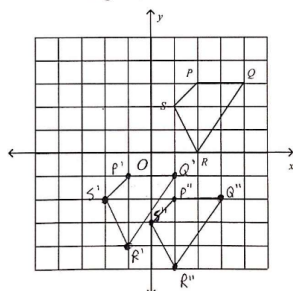


b)  $(x, y) \rightarrow (x, y - 3)$



5. Quadrilateral PQRS is plotted on the grid below.

a) On the graph, draw the translation of polygon PQRS three units to the left and four units down. Label the image P'Q'R'S'.



b) Now create polygon P''Q''R''S'' by translating polygon P'Q'R'S' using the rule  $(x, y) \rightarrow (x + 2, y - 1)$ . List the coordinates of P''Q''R''S'' below

P'' (1, -2) Q'' (3, -2) R'' (1, -5) S'' (0, -3)

c) Write a general rule which translates polygon PQRS to polygon P''Q''R''S''.

$(x, y) \rightarrow (x - 1, y - 5)$

## Transformations Day 2 - Reflections

### Learning Target:

Coordinate Geometry: Transformations

a. I can apply ordered pair rules to basic translations, rotations and reflections.

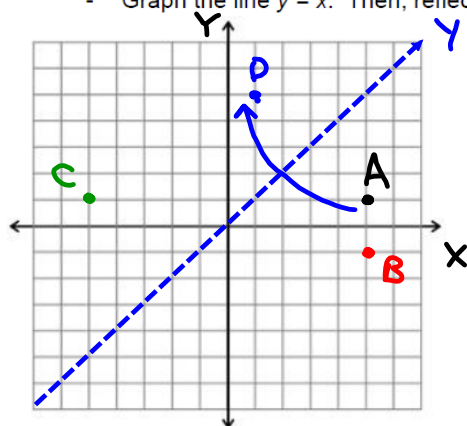
# Definitions:

**REFLECTIONS:** A transformations which creates a mirror image of a given pre-image over a given line.

**LINE OF REFLECTION:** The line over which a pre-image is reflected over.

On the coordinate plane below...

- Graph the coordinate pre-image (5, 1) and label it with the letter A.
- Reflect point A over the x-axis and label that image B.
- Reflect point A over the y-axis and label that image C.
- Graph the line  $y = x$ . Then, reflect point A over the line  $y = x$  and label that image D.



Start (5, 1)

List the coordinates of each of the resulting images:

Coordinates of image of B: ( 5 , -1 ) x-axis

Coordinates of image of C: ( -5 , 1 ) y-axis

Coordinates of image of D: ( 1 , 5 )  $y = x$

# Reflection Transformation Rules:

In general, list the transformation rule for each of the following reflections:

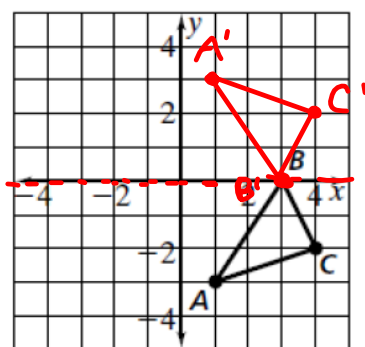
Over the x-axis:  $(x, y) \rightarrow (x, -y)$

Over the y-axis:  $(x, y) \rightarrow (-x, y)$

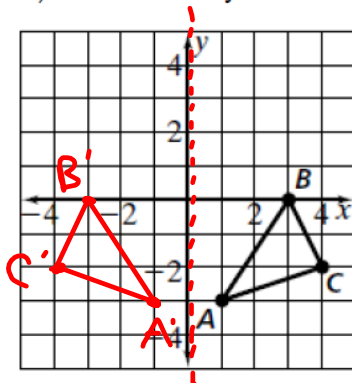
Over the line  $y = x$ :  $(x, y) \rightarrow (y, x)$

1. Reflect the triangle below over each of the following lines. Label the images  $\triangle A'B'C'$

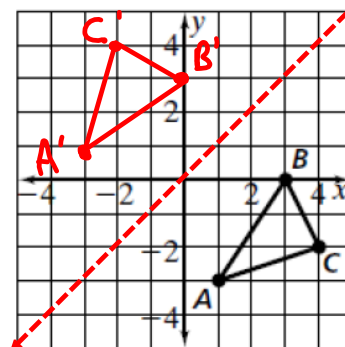
a) Over the x-axis.



b) Over the y-axis.

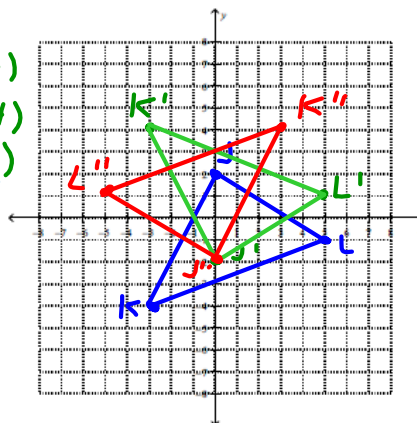


c) Over the line  $y = x$ .



2. a) Draw  $\triangle JKL$  which has coordinates  $J(0,2)$ ,  $K(-3,-4)$ , and  $L(5,-1)$ .  
 b) Draw the image  $\triangle J'K'L'$  after a reflection of  $\triangle JKL$  over the  $x$ -axis.  
 c) List the coordinates of  $\triangle J'K'L'$ .

$$\begin{array}{lcl} J(0,2) & \rightarrow & J'(0,-2) \\ K(-3,-4) & \rightarrow & K'(-3,4) \\ L(5,-1) & \rightarrow & L'(5,1) \end{array}$$



- d) Draw the image  $\triangle J''K''L''$  after a reflection of  $\triangle J'K'L'$  over the  $y$ -axis.

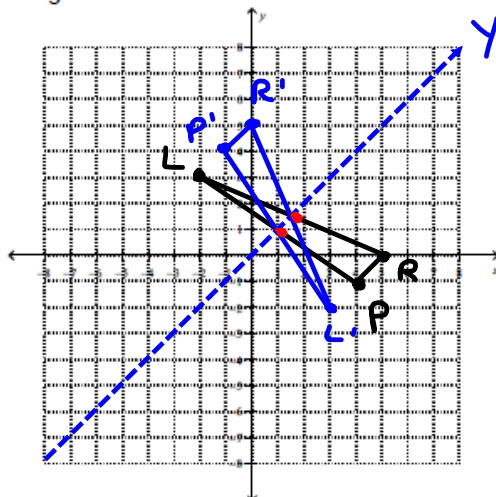
$$\begin{array}{lcl} J'(0,-2) & \rightarrow & J''(0,-2) \\ K'(-3,4) & \rightarrow & K''(3,4) \\ L'(5,1) & \rightarrow & L''(-5,1) \end{array}$$

$$(-x, y)$$

Would the final image be different if the reflections were done in the opposite order?

Is this always true?

3. a) Draw  $\triangle PRL$  which has coordinates  $P(4,-1)$ ,  $R(5,0)$ , and  $L(-2,3)$ .  
 b) Draw the image  $\triangle P'R'L'$  after a reflection of  $\triangle PRL$  over the line  $y = x$ .



$$\begin{array}{l} y = x \\ (x, y) \rightarrow (y, x) \\ P'(-1, 4) \\ R'(0, 5) \\ L'(3, -2) \end{array}$$

Example 4:

a) Draw  $\triangle ABC$  which has coordinates  $A(0,1)$ ,  $B(3,4)$ , and  $C(5,1)$ .

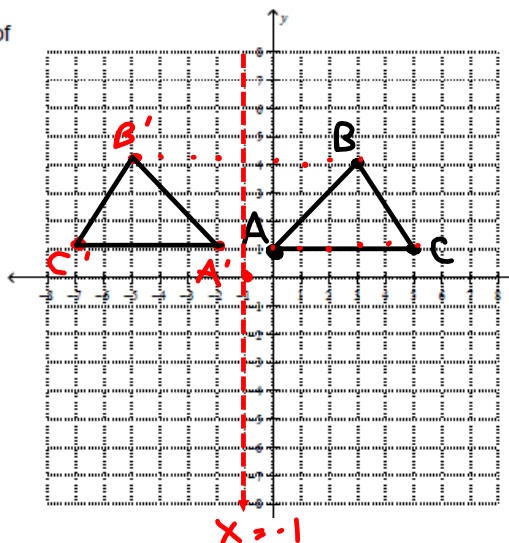
b) Draw the image  $\triangle A'B'C'$  after a reflection of  $\triangle ABC$  over  $x = -1$ .

c) List the coordinates of  $A'B'C'$ .

$A$  (0, 1)  $\rightarrow$   $A'$  \_\_\_\_\_

$B$  (3, 4)  $\rightarrow$   $B'$  \_\_\_\_\_

$C$  (5, 1)  $\rightarrow$   $C'$  \_\_\_\_\_



The line  $x = -1$   
is a vertical line.

$y = mx + b$   
 $y = c$        $x = c$   
horizontal      vertical

Example 5:

a) Draw  $\triangle ABC$  which has coordinates  $A(0,1)$ ,  $B(3,4)$ , and  $C(5,-3)$ .

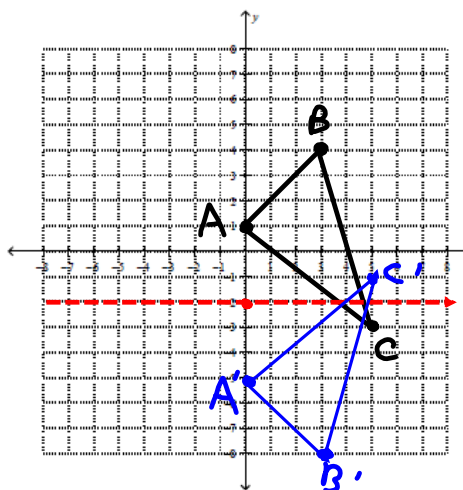
b) Draw the image  $\triangle A'B'C'$  after a reflection of  $\triangle ABC$  over  $y = -2$ .

c) List the coordinates of  $A'B'C'$ .

$A$  (0, 1)  $\rightarrow$   $A'$  (0, -5)

$B$  (3, 4)  $\rightarrow$   $B'$  (3, -8)

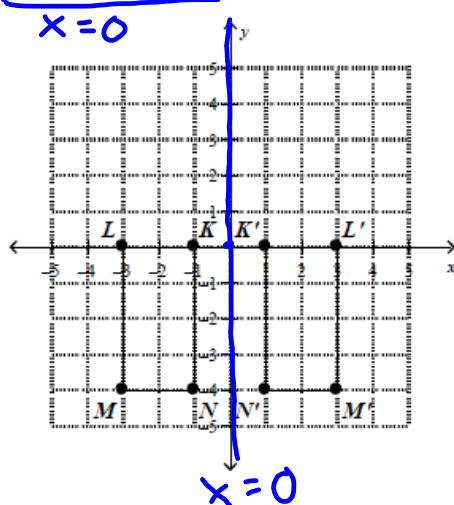
$C$  (5, -3)  $\rightarrow$   $C'$  (5, -1)



The line  $y = -2$   
is horizontal.

Example 6:

Draw the line of reflection which caused rectangle  $KLMN$  to reflect onto rectangle  $K'L'M'N'$ .  
What is the equation of the line of reflection?



Example 7:

Draw the line of reflection which caused triangle  $ABC$  to reflect onto triangle  $A'B'C'$ . What is the equation of the line of reflection?

