

## Warm-Up

1. Find the height and slant height of the pyramid if the volume of the pyramid is 4096 in<sup>3</sup>.

$$V = \frac{Bh}{3}$$

$$4096 = \frac{1024h}{3} \cdot 3$$

$$12^2 + 16^2 = l^2$$

$$400 = l^2$$

$$20 = l$$

$$B = 1024$$

$$12 = h$$

$$12 \text{ in}$$

## Warm-Up

2. Find the volume of a cone with a diameter of 20 cm and a height of 16 cm.

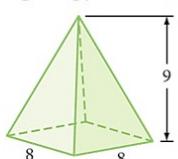
ANSWERS

11.3

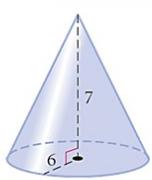
## Exercises

Find the volume of each solid named in Exercises 1–6. All measurements are in centimeters.

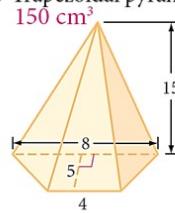
1. Square pyramid  $192 \text{ cm}^3$



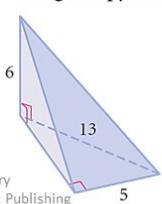
2. Cone  $84\pi \text{ cm}^3 \approx 263.9 \text{ cm}^3$



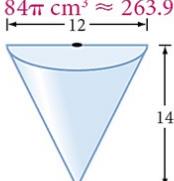
3. Trapezoidal pyramid  $\frac{1}{3} 150 \text{ cm}^3$



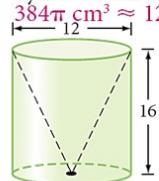
4. Triangular pyramid  $60 \text{ cm}^3$



5. Semicircular cone  $\frac{84\pi}{3} \text{ cm}^3 \approx 263.9 \text{ cm}^3$



6. Cylinder with cone removed  $\frac{1}{3} 384\pi \text{ cm}^3 \approx 1206 \text{ cm}^3$



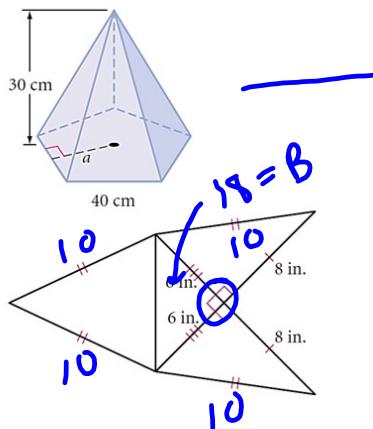
## ANSWERS

## 11.3 Exercises

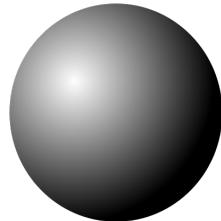
- 14.** Bretislav has designed a crystal glass sculpture. Part of the piece is in the shape of a large regular pentagonal pyramid, shown at right. The apothem of the base measures 27.5 cm. How much will this part weigh if the glass he plans to use weighs 2.85 grams per cubic centimeter?

78,375 grams

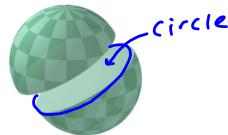
- 15.** Jamala has designed a container that she claims will hold 50 in.<sup>3</sup>. The net is shown at right. Check her calculations. What is the volume of the solid formed by this net? *(h)*

48 in.<sup>3</sup>
Sections 11.6 and 11.7  
 Surface Area and Volume of Spheres


**SPHERE:** A solid, round figure, where all points on the surface are the same distance from its center.



**HEMISPHERE**: half of a sphere.

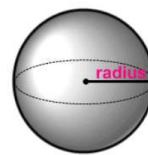
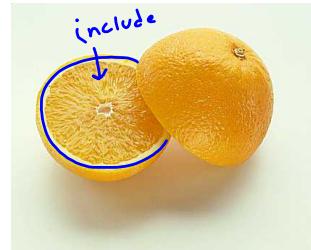


Northern Hemisphere

Southern Hemisphere

Western Hemisphere

Eastern Hemisphere



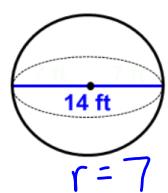
$$\text{SURFACE AREA OF A SPHERE} = 4\pi(\text{radius})^2$$

$$SA = 4\pi r^2$$

Examples

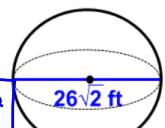
Find the surface area of the sphere or hemisphere.

1.



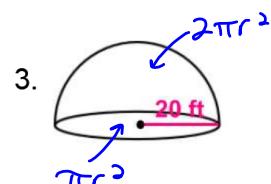
$$\begin{aligned} SA &= 4\pi r^2 \\ SA &= 196\pi \text{ ft}^2 \end{aligned}$$

2.



$$\begin{aligned} r &= 13\sqrt{2} \\ SA &= 4\pi(13\sqrt{2})^2 \\ SA &= 1352\pi \text{ ft}^2 \end{aligned}$$

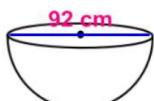
3.



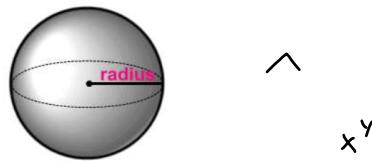
$$\begin{aligned} 2\pi r^2 \\ \pi r^2 \end{aligned}$$

$$\begin{aligned} 2\pi(20)^2 + \pi(20)^2 \\ 800\pi + 400\pi = 1200\pi \text{ ft}^2 \\ \underline{\underline{V_{\text{Hemisphere}} = 3\pi r^2}} \\ = 3\pi(20)^2 = 1200\pi \text{ ft}^3 \end{aligned}$$

4.



$$\begin{aligned} SA &= 3\pi r^2 \\ SA &= 3\pi(46)^2 \\ SA &= 6348\pi \text{ cm}^2 \end{aligned}$$



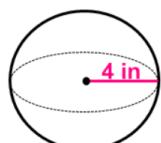
$$\text{VOLUME OF A SPHERE} = \frac{4\pi(\text{radius})^3}{3}$$

$$V = \frac{4\pi r^3}{3}$$

### Examples

Find the volume.

5.



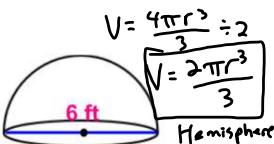
$$V = \frac{4\pi(4)^3}{3}$$

$$V = \boxed{85.\overline{3}\pi \text{ in}^3}$$

or  
 $\boxed{85\frac{1}{3}\pi \text{ in}^3}$

or  
 $\boxed{\frac{256\pi}{3} \text{ in}^3}$

6.



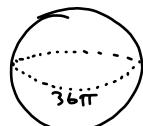
$$V = \frac{4\pi r^3}{3} \div 2$$

$$V = \frac{4\pi(3)^3}{3} \div 2$$

$$V = 36\pi \text{ ft}^3 \text{ (whole sphere)}$$

$$V_{\text{Hemisphere}} = \frac{36\pi}{2} = \boxed{18\pi \text{ ft}^3}$$

7. Circumference of ~~Sphere~~ =  $36\pi$  cm.



$$C = 2\pi r$$

$$36\pi = 2\pi r$$

$$18 = r$$

$$V = \frac{4\pi(18)^3}{3}$$

$$V = 7776\pi \text{ cm}^3$$

8. Surface Area of a Sphere =  $900\pi \text{ ft}^2$ .

$$SA = 4\pi r^2$$

$$900\pi = 4\pi r^2$$

$$225 = r^2$$

$$15 = r$$

$$V = \frac{4\pi(15)^3}{3}$$

$$V = 4500\pi \text{ ft}^3$$

## Assignment: 11.6 and 11.7 SA and Volume of Spheres HW